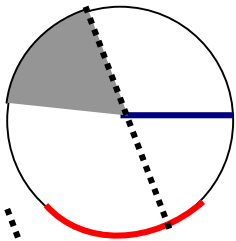


# Circle Theorems

A circle has many parts



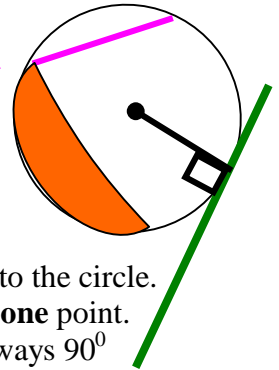
This is the **Diameter**.



This is a **Sector**.

This is a **Chord**.

— This is the **Radius**.



This line is a **Tangent** to the circle.

A Tangent touches a circle at **one** point.

The angle between the Tangent and the Radius is always  $90^\circ$

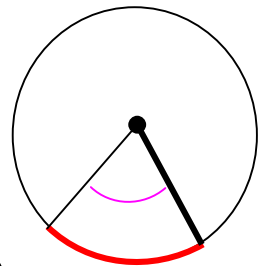


This is known as a **Segment**. Like an orange segment.

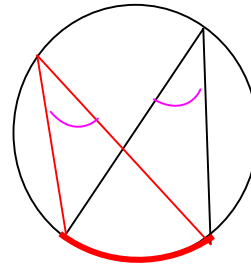
This is an **Arc**.



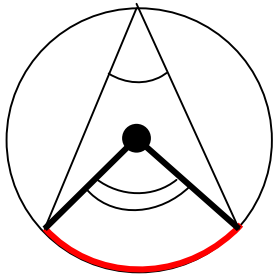
An arc will **subtend** an angle at the **centre** of a circle.



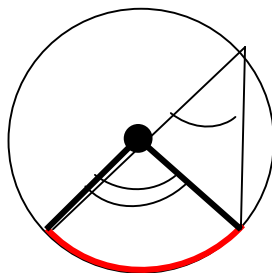
The arc may also subtend angles at different points on the circumference of the circle.



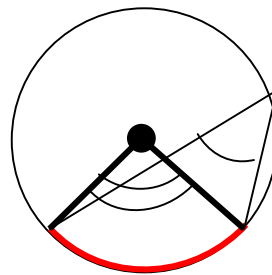
**RULE 1** The angle subtended by an arc at the centre of a circle is equal to **twice** the angle subtended by the same arc at the circumference.



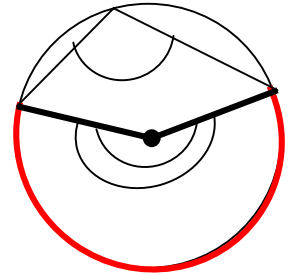
**Like a Tent**



**Blown sideways**

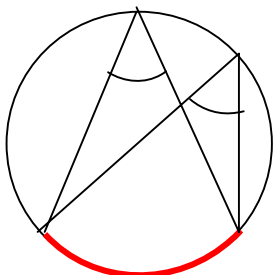


**Blown more sideways**

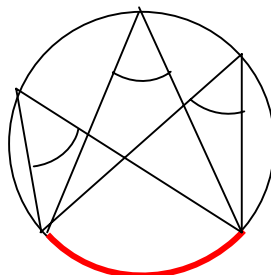


**Blown inside out.**

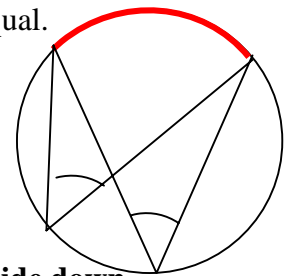
**RULE 2** The angles subtended by an arc on the circumference of the circle are equal.



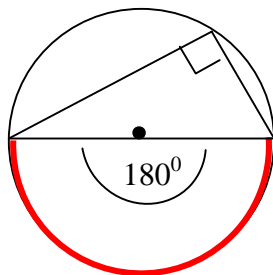
**Like mountain peaks.**



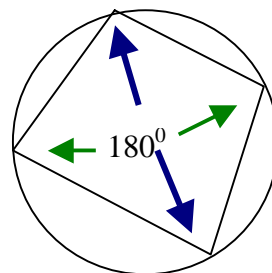
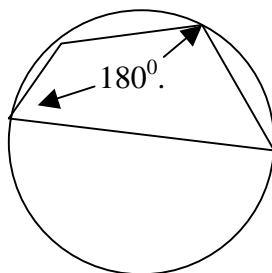
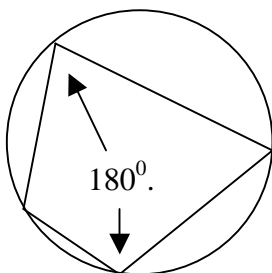
**Even upside down.**



**RULE 3** The angle in a semicircle is always  $90^\circ$ . Of course it is: It is half the angle at the centre which is  $180^\circ$ .

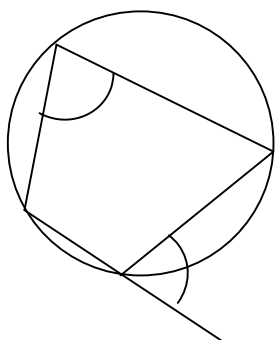


**RULE 4** Concerns Cyclic Quadrilaterals. Quadrilateral which have all their vertices on the Circumference of a circle.



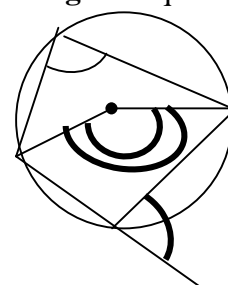
The opposite angles in a cyclic quadrilateral are **supplementary**. They add up to  $180^\circ$ .

Continuing any one line of the quadrilateral produces an **exterior angle**.



**RULE 5** In a cyclic quadrilateral, The **exterior angle** is equal to the **interior opposite angle**.

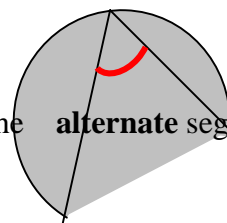
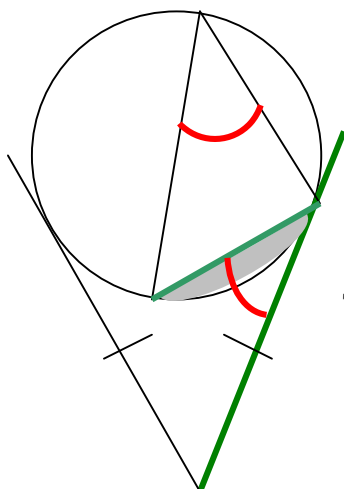
The exterior angle is also **half** the angle at the centre. Try and figure out why!



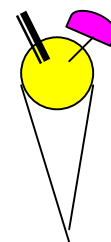
**Tangents, chords and segments**

The **chord** forms a segment with the circle and an **angle** with the **tangent**.

This angle is equal to the **angle in** the **alternate segment**.



**Two tangents** from a point outside a circle **are equal** in length. Like an ice cream cone!



Yum Yum!

